

# Efficient Route Planning

## SS 2011

Lecture 12, Friday August 5<sup>th</sup>, 2011  
(Course evaluation results, Transfer Patterns II)

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# Overview of this lecture

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- Organizational
  - Your results from [Ex. Sheet #8 \(Transfer Patterns\)](#)
  - Summary of your evaluation of the whole course
  - This is the **last** lecture
- Transfer patterns
  - Short recap
  - The direct-connection data structure
  - Feasible pre-computation using important stations
- Exam
- Current work at the chair

# Feedback from ES#8 (Transfer Patterns)

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## ■ Summary / excerpts

**Stand 5.8 2:38**

- Aufgabe 1 (Evaluationsbogen) mit Hingabe ausgeführt
- Gute Idee das zu belohnen
- Ansonsten haben nur wenige die Aufgabe gemacht wegen keine Zeit und schon genug Punkte

# Course evaluation results 1/5

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- Contents of the course
  - Very interesting & relevant topic and algorithms (many)
  - Very practical, that's good (many)
  - Good balance between theory and practice (several)
  - Google Maps stuff was interesting (several)

## ■ Style of the course

- Competent and interesting explanations (many)  
... but sometimes not in the first attempt (several)
- Good, relaxed atmosphere (many)  
... manchmal etwas zu viel "Späße" (one)
- Much interaction with students (many)
- Doing drawings / proofs "online" is instructive (several)
- Implementation advice / live programming helps (several)  
... "watching someone for 30 minutes trying to fix the code is a waste of everyone's time" (one)

# Course evaluation results 3/5

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## ■ Exercises 1/2

- Very interesting but also very time-consuming (many)  
... but with the extra weeks it was ok (several)
- Implementing very useful for understanding (many)  
"By implementing all the algorithms, you really learn something for lifetime"
- Give more implementation advice earlier on (many)  
... a lot of time spent in refactoring of old code (several)
- Experimentation results were interesting / incentive (several)  
... Experimentation results useless without clear params (one)

# Course evaluation results 4/5

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## ■ Exercises 2/2

- More feedback on the code would have been nice (several)
  - "Hire more tutors which can actually help with the code" (one)
  - "Offer a tutorial to discuss problems with the exercises. Sometimes questions are too complicated for a Forum" (one)
- A lot of unnecessary code to write (one)
  - "While it was stated that it was considered to be a valuable part of the learning process, it felt more like an excuse for not having prepared anything on the lecturers part."
- "It felt like we are doing one algorithm after the other" (one)

# Course evaluation results 5/5

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## ■ Other

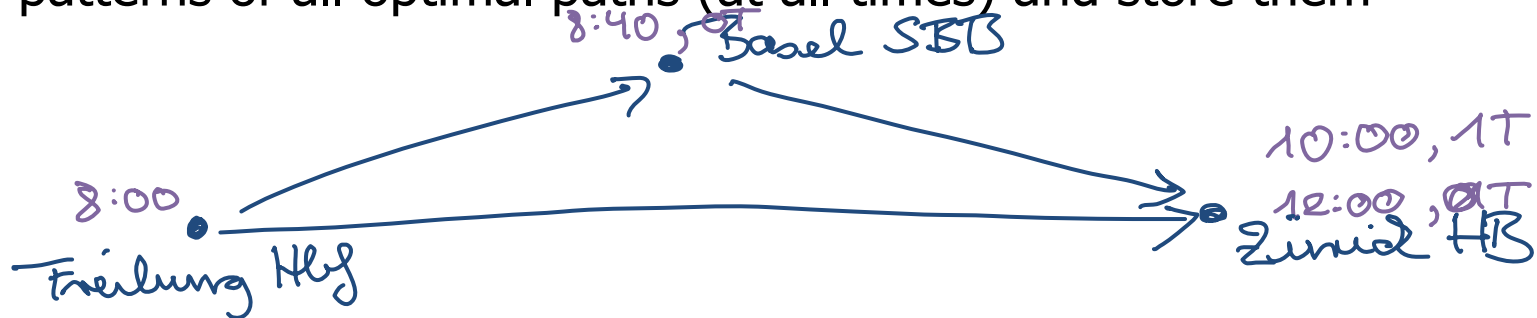
- Video recordings were extremely helpful (many)
- Java programmers had a big disadvantage (many)
  - "Als Javanutzer fühlt man sich ein wenig wie der Depp"
  - "Viele Implementierungsvorschläge gehen nur in C (hash map)"
- The grade should depend on the exercise solutions (one)
- Having an exam for this kind of lecture seems odd (one)
- See other people's code after the deadline (one)



# Transfer Patterns

## ■ The basic idea on one slide

- The **transfer pattern** of a path = the sequence of stations on the path where one boards, transfers, or alights
- Idea: for each pair of stations, precompute all transfer patterns of all optimal paths (at all times) and store them



- Then, at query time, do a time-dependent Dijkstra computation on this so-called **query graph**, where each arc evaluation is again a shortest path query, but restricted to **no transfers**
- Such **direct-connection** queries are easy to compute fast

# Components of a Transfer Pattern Router

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- **Transfer patterns precomputation**
  - Compute (parts of) all transfer patterns of all optimal paths
- **Direct-connection tables precomputation**
  - Compute data structure for fast direct connection queries
- **Query Graph Construction**
  - Build the query graph of all transfer patterns between **A** and **B**
- **Query Graph Evaluation**
  - Dijkstra search on query graph, with arcs = direct connections
- **Various Refinements / Optimizations**
  - For example: filter out rare transfer patterns, ...

# Direct-Connection Queries

- One table per "line", let's call this line L17

Stations:	S154	S97	S987	S111	...
Time from start:	0min	7min	12min	21min	...
Start times:	8:15	9:15	10:15	11:20	12:20 ...

- Lines per station ... with positions in the respective line table

Station S97:	(L8, 4)	(L17, 2)	(L34, 5)	(L87, 17)	...
Station S111:	(L9, 1)	(L13, 5)	(L17, 4)	(L55, 16)	...

- Example query ... from S97 @ 10:20 to S111

- Intersect the lists of the two stations : (L17, 2 → 4) ...
- Find time from start to S97 and to S111 : 7min and 21min
- Find first start time after 10:20 – 7min : 10:15 → **depart 10:22**
- Compute arrival time at S111 : 10:15 + 21min → **arrive 10:36**

# Important Stations 1/3

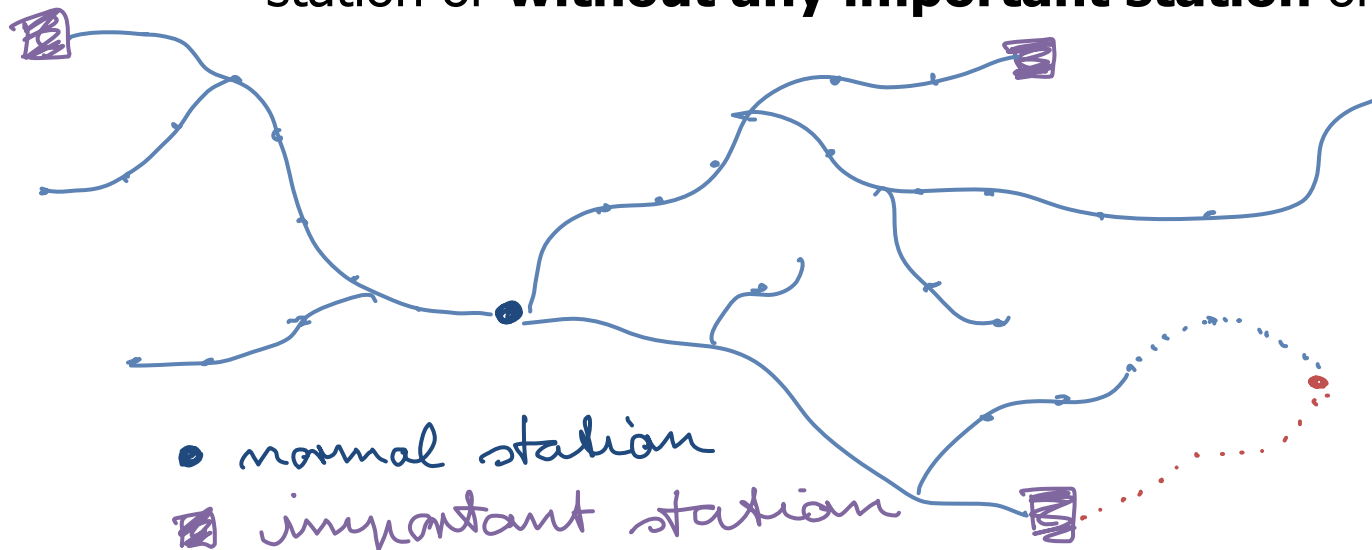
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- The pre-computation so far is quadratic
  - Full Dijkstra to the whole graph for every station
  - Let  $m = \text{\#stations}$  and  $n = \text{\#nodes}$
  - This amounts to a total of  $\sim m \cdot n \cdot L$  Dijkstra iterations where  $L$  is the average number of labels per node
  - A multi-label Dijkstra is  $\approx 10$  times slower per iteration than an ordinary Dijkstra (due to label set maintenance)
  - Example 1:  $m = 10\text{K}$ ,  $n = 1\text{M}$ ,  $L = 3$ ,  $10 \mu\text{s}$  / Dijkstra iter.  
30K seconds  $\approx$  **80 hours**
  - Example 2:  $m = 1\text{M}$ ,  $n = 1\text{G}$ ,  $L = 3$ ,  $10 \mu\text{s}$  / Dijkstra iter.  
3G seconds  $\approx$  **8 million hours  $\approx$  1000 years**

# Important Stations 2/3

## ■ How to improve on this?

- Idea: Select **1%** of all stations as “important”
- Heuristic: where many paths transfer + geographic diversity
- For each **important** station compute a **global Dijkstra** as before
- For each **non-important** station, compute a **local Dijkstra**, that is, compute all **local paths** = all paths **until an important station** or **without any important station** on them



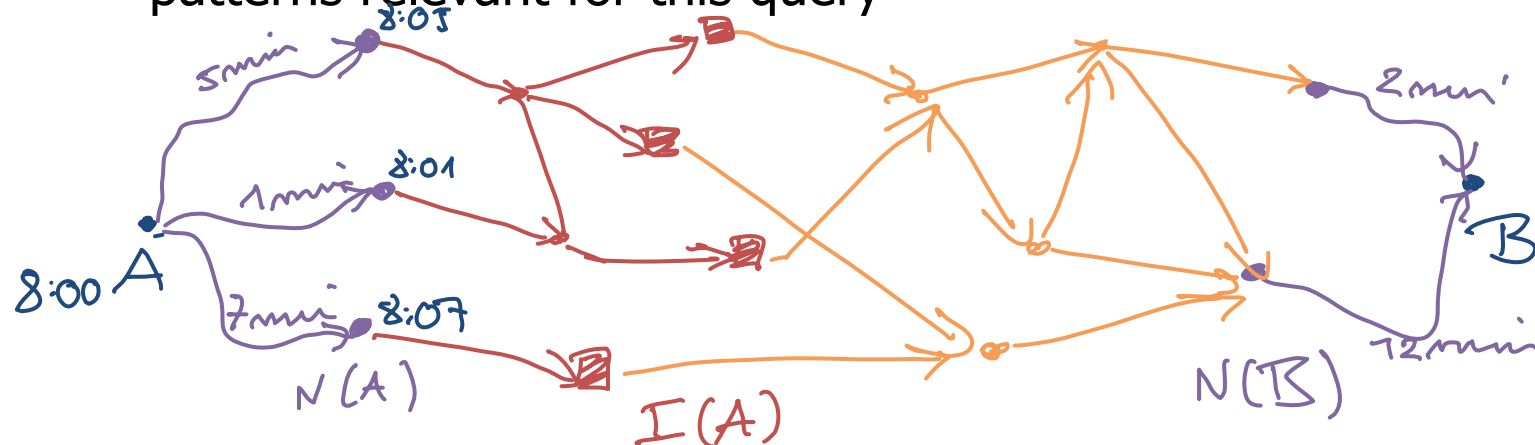
# Important Stations 3/3

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- Local Dijkstra search from a station  $s$  ... problem:
  - The number of (nodes on the) local paths is indeed small
  - But we have the usual "15 hours to the next village problem":  
If only one of the local paths has a large cost, say **15 hours**, then the Dijkstra computation needs to search everything that can be reached from  $s$  within **15 hours**
  - Unfortunately, almost every station has at least one local path of high cost, and hence our local Dijkstra searches end up being no less expensive than the global Dijkstra searches
  - Simple heuristic remedy: only consider local paths **up to two transfers**, that is, paths where more than two transfers are needed to get to an important station will be lost
  - Experience shows that these are **very rare** in practice

# Query graph construction (sketch)

- For given source and target location A and B
  - Compute the sets  $N(A)$  and  $N(B)$  of stations near A and B
  - Get the precomp. local transfer patterns of these stations
  - Get the sets  ~~$I(A)$  and  $I(B)$~~  of important stations where the local paths from A ~~and from B~~ end
  - Get the global transfer patterns for each ~~pair of~~ important stations  ~~$(a, b)$~~  where  $a \in I(A)$  ~~and  $b \in I(B)$~~
  - Assemble this to form the query graph of all transfer patterns relevant for this query



# Query graph search

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- Time-dependent Dijkstra search
  - Start at the source location
  - For arcs from the source location to nearby station  
launch road network query (or have these precomputed)  
Same for arcs to the target location
  - For arcs between stations, ask direct-connection table



# Exam 1/2

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- The exam will be on Monday, August 15 at 2:00 pm
  - Here in HS 026 + it will last (only) 90 minutes
  - There will be **4 tasks**, out of which you can select **3 tasks**
  - Three **kinds** of tasks are possible
    - Execute an algorithm from the lecture, or some variant of it, on a given example (on paper)
    - Write a small program to solve a variant of a problem we have seen in the lecture
    - Compute, reason about, or prove a non-trivial (but also not very difficult) property of an algorithm or data structure from the lecture, or some variant of it
  - See the [Search Engines WS 2009/2010 exam](#) for examples

# Exam 2/2

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- The **bachelor students** (and only those)
  - ... must take an oral exam
  - On *Wednesday, August 17*, starting from 2:00 pm
  - In my office: *building 51, 2nd floor, room 028*
  - Questions will be of a similar kind as in the written exam, but of course not exactly the same

# Work in my group

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## ■ Chair for Algorithms and Data Structures

- Our work roughly subdivides as
  - 1/3 theory (new algorithms, complexity analysis, etc.)
  - 1/3 algorithm engineering (efficient implementations)
  - 1/3 software engineering (good, durable software)
- Current projects
  - Route planning
  - Search engines, in particular: [CompleteSearch](#) & [Broccoli](#)
- Current readings
  - <http://ad.informatik.uni-freiburg.de/papers>

# References

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## ■ Transfer Patterns

Fast Routing in Very Large Transportation Networks  
using Transfer Patterns

Bast, Carlsson, Eigenwillig, Geisberger, Harrelson,  
Rachyev, Viger ESA 2010

<http://www.springerlink.com/content/c873271685124v42/>

<http://ad.informatik.uni-freiburg.de/papers>

