

# Efficient Route Planning

## SS 2011

Lecture 9, Friday July 15<sup>th</sup>, 2011  
(Transit Networks, GTFS)

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# Overview of this lecture

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## ■ Organizational

- Your feedback from [Ex. Sheet #6](#) (transit node routing)

## ■ Transit Networks

- In the US, "transit" means "public transportation"
- Transit node routing has nothing to do with this "transit"
- We will see how to model a transit network
- GTFS = General Transit Feed Specification
- Do our algorithms so far work on transit networks?
  
- [Exercise Sheet #7](#): Parse a transit network from GTFS and run Dijkstra on it, and if possible, your other alg's too

# Feedback on ES#6 (transit node routing)

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- Summary / excerpts

Stand 15.7 12:59

- Noch beim Debuggen von contraction hierarchies
- Gerade Endsemesterstress bei vielen

# Coding standards

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- Sind jetzt auch für **Java** ausgearbeitet
  - Siehe Link auf Ihrer Daphne-Seite  
<https://daphne.informatik.uni-freiburg.de/svn/CodingStandards/>
  - Sie finden dort
    - Eine **README.deutsch.txt**
    - Ein vollständiges Code-Beispiel für **C++**
    - Ein vollständiges Code-Beispiel für **Java**
    - Für eigene Projekte, einfach den entsprechenden Ordner kopieren und Code schreiben, sollte dann gehen

# Transit Networks

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- What kind of data have we got?
  - Stations (train stations, bus stops, etc.)
  - Lines (trains, buses, trams, etc.)
  - The schedule of these lines, that is, on which days do they serve which stations at which times
  - Since we want to compute shortest path queries also for transit networks (best way to get from **A** to **B**), we want to model them as (directed) graphs, too, just like road networks ... but how?

# Time-dependent model 1/2

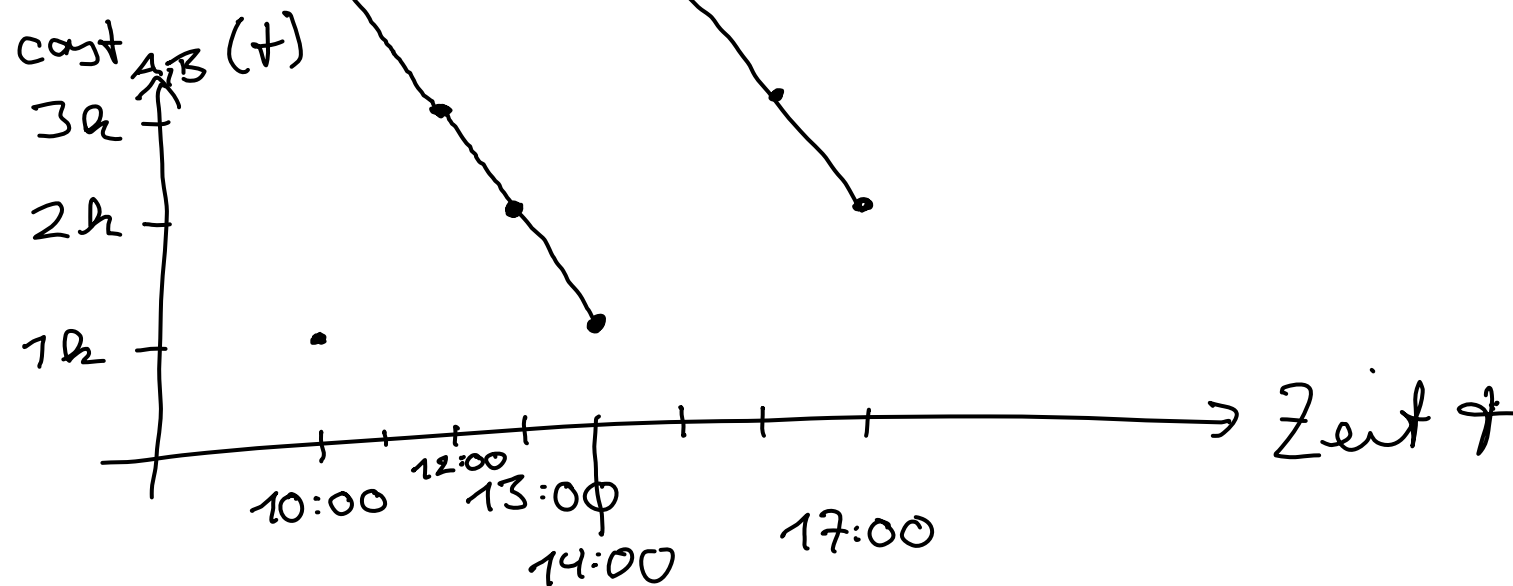
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- The first thing that comes to mind
  - Each station is a **node**
  - There is an **arc** between two nodes **u** and **v**, if there is a vehicle (train, bus, tram, ...) going **non-stop** from **u** to **v**
  - However, that arc can only be used at certain times, and the time it takes to travel across the arc depends on the vehicle commuting at that time
  - We can model this via a cost function for each arc **(u, v)**  
 $\text{cost}_{u,v}(t)$  = the time to get from **u** at time **t** ... to **v**

# Time-dependent model 2/2

## ■ Example

- Stations **A** and **B** with two lines **L1** and **L2**
- **L1** takes **1** hour from **A** to **B** (non-stop) and departs from **A** at **10:00**, **14:00** and **18:00**
- **L2** takes **2** hours from **A** to **B** (non-stop) and departs from **A** at **13:00** and **17:00**



# Time-dependent Dijkstra 1/2

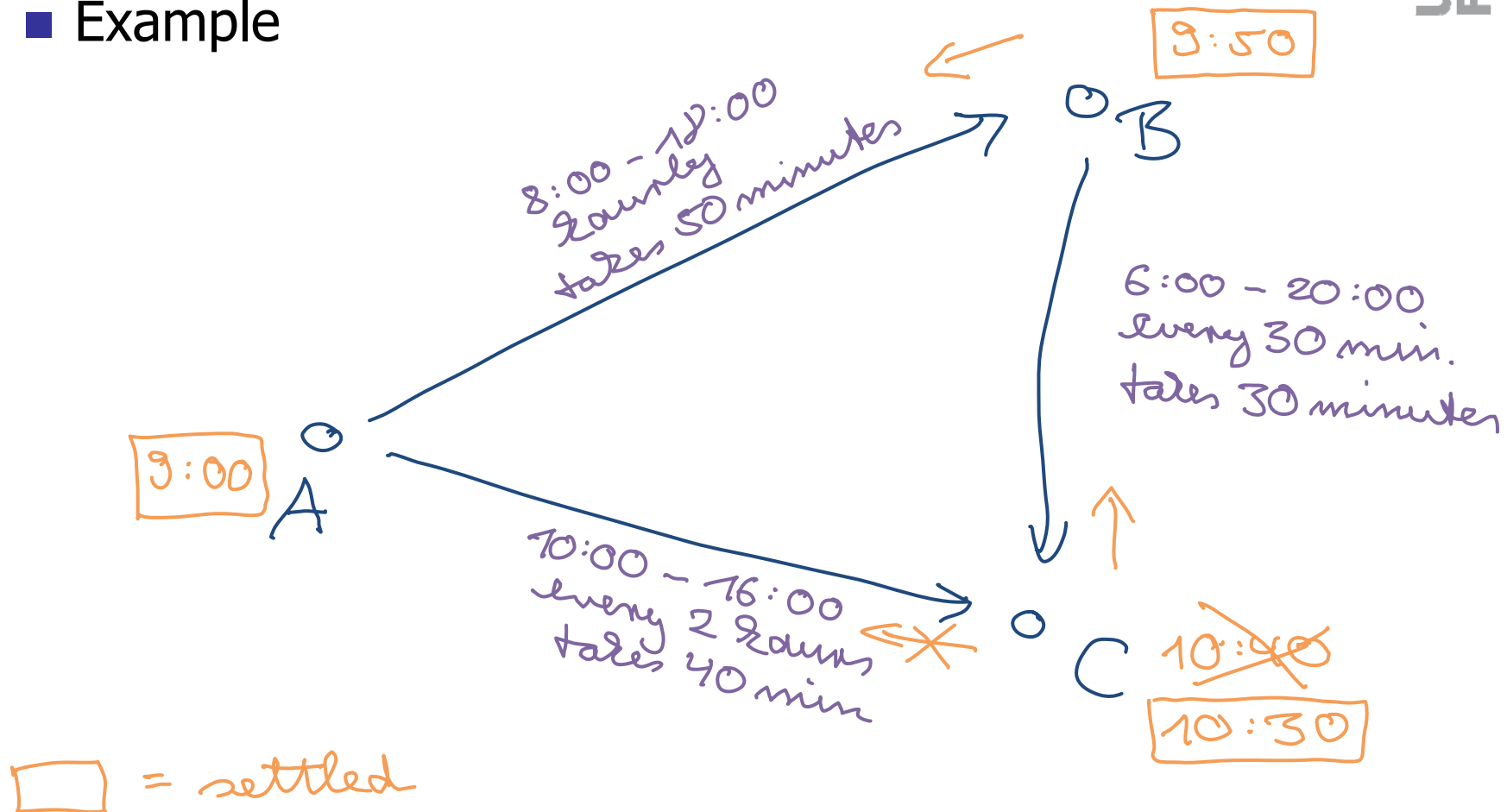
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- How to compute shortest paths on such a graph?
  - A simple variant of Dijkstra's algorithm does it
  - Tentative distances at the nodes are now **times of day**
    - We will store **absolute** times (like 10:20) and call them  $t[u]$  for node  $u$ , but we could also store times relative to the start time (like 40 minutes)
  - Start with  $t[s] = \text{start time}$  and all other  $t[u] = \infty$
  - When relaxing an arc  $(u, v)$  we compute  $c = c_{u,v}(t[u])$  and take  $t[v] = t[u] + c$  if that improves on the previous  $t[v]$
  - As for ordinary Dijkstra process the node  $u$  with the smallest  $t[u]$  next, and stop when this is the target node



# Time-dependent Dijkstra 2/2

## ■ Example



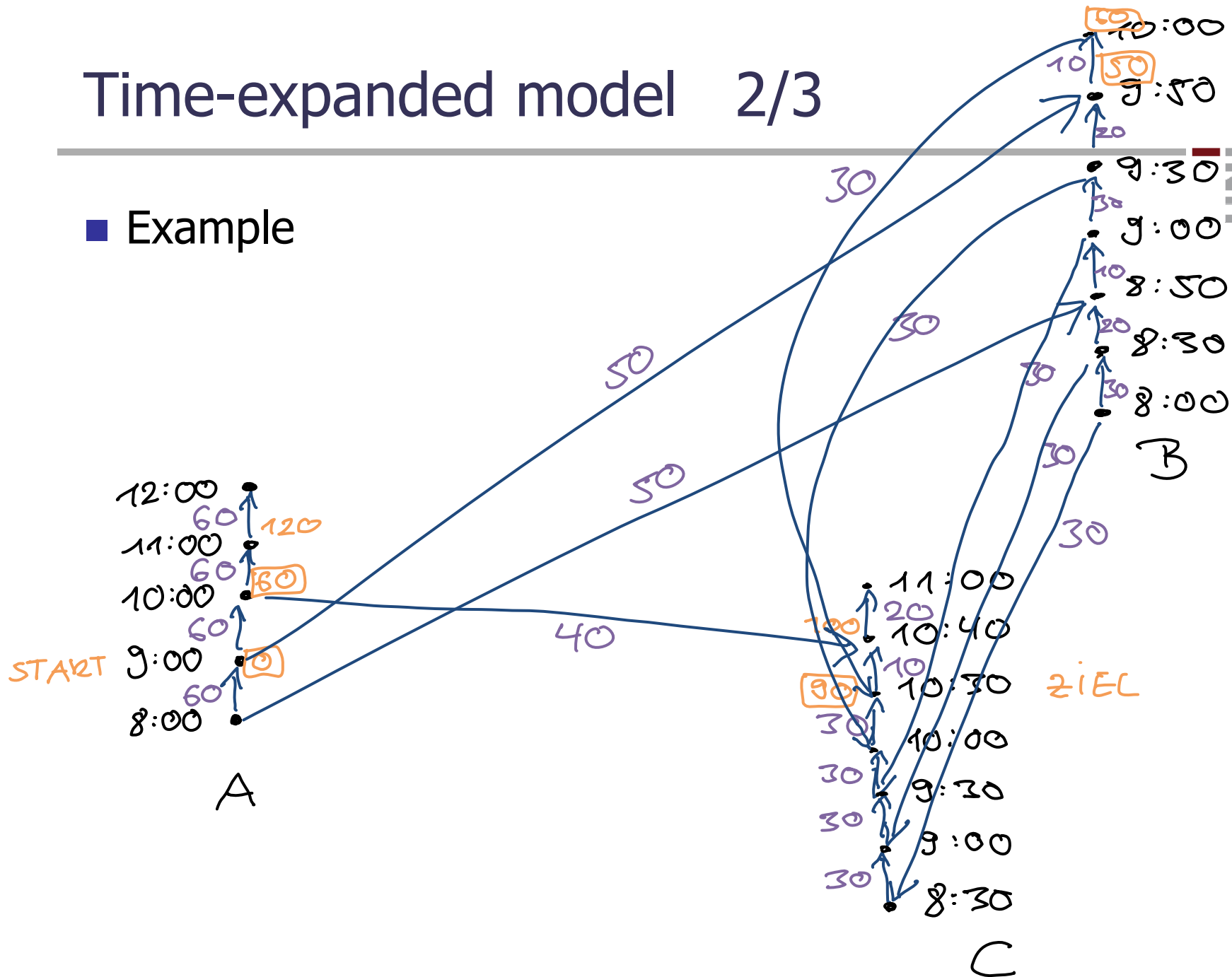
# Time-expanded model 1/3

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- A node = a particular time at a particular station
  - Only at times, where something (= an arrival or a departure) is happening
  - For example, Freiburg Hbf @ 13:57
  - There is an arc between two nodes  $A@t_1$  and  $B@t_2$  if there is a vehicle departing from  $A$  at time  $t_1$  and arriving at  $B$  at time  $t_2$ , without stops inbetween
  - The cost of the arc is simply the travel time  $t_2 - t_1$
  - There is also an arc from  $A@t_1$  to that node  $A@t_2$  with the smallest  $t_2 > t_1$  ... we call these **waiting** arcs

# Time-expanded model 2/3

■ Example



# Time-expanded model 3/3

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- How do we compute shortest paths in this model?
  - It's an ordinary directed graph with non-negative arc costs, so we can use ordinary Dijkstra
  - Only problem: we do not have a target node, we only have a target station
  - Solution: Run Dijkstra until anyone node from the target station is settled (which will be the first one reached)

# Time-expanded vs. time-dependent

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- So far, not much difference
  - Given a query  $A@t \rightarrow B$ , consider the sequence of arcs relaxed by a (time-dependent) Dijkstra on the time-dependent graph
  - The Dijkstra on the time-expanded graph relaxes the same arcs in the same order, **plus** some additional waiting arcs to some additional nodes and the arcs leaving from these nodes
  - Intuitively, the time-dependent Dijkstra considers waiting and normal arcs in one (time-dependent) arc
  - The big advantage of the time-expanded model is that we have an ordinary directed graph and can thus use all our previous algorithms on it

# Advanced modelling issues

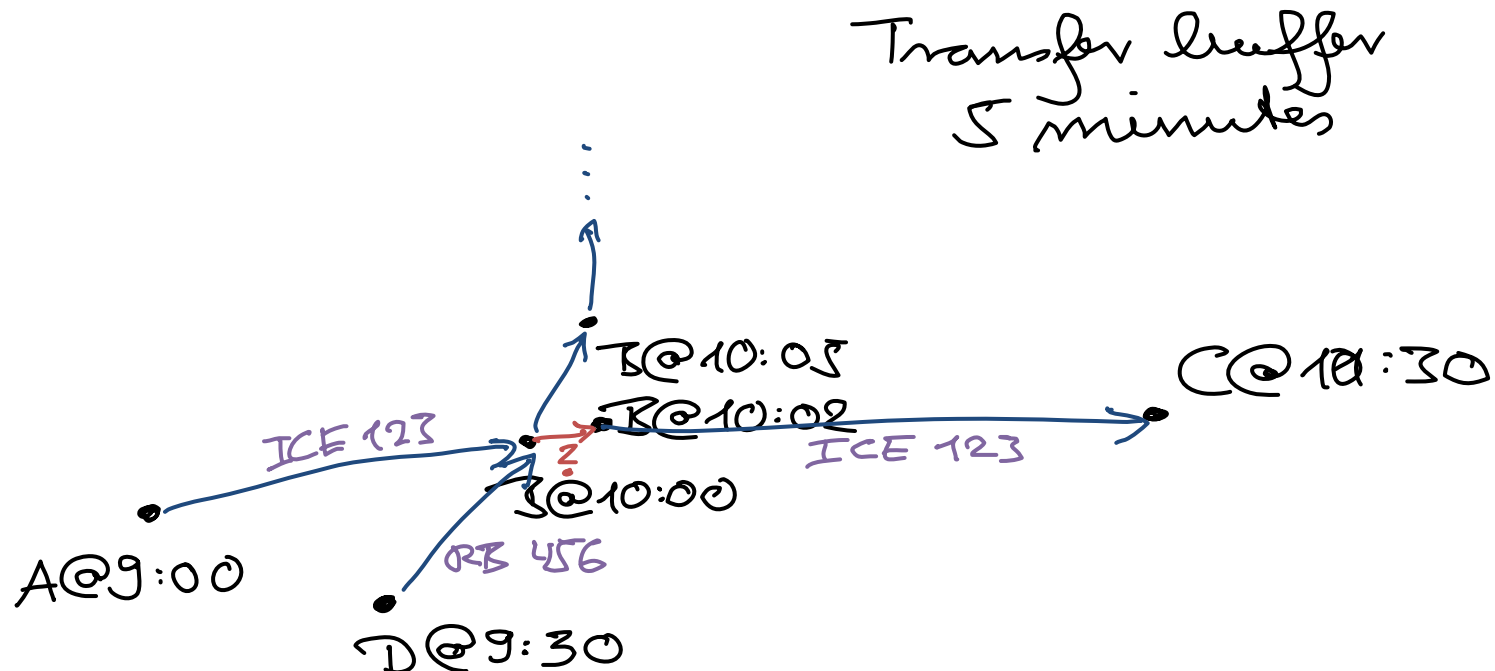
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- For example, what about ...
  - Transfer buffers
    - We need a minimal amount of time to transfer between two vehicles → next slide
  - Service days
    - Different schedules on different weekdays, holidays, etc. → later slide
  - Multi-criteria cost functions
    - Maybe we can get from A@t to B in 3 hours with 0 transfers, or in 2 hours with 2 transfers
    - Which one is better depends on user preference, so we should compute both → next lecture

# Transfer buffers 1/5

## ■ Time-expanded model

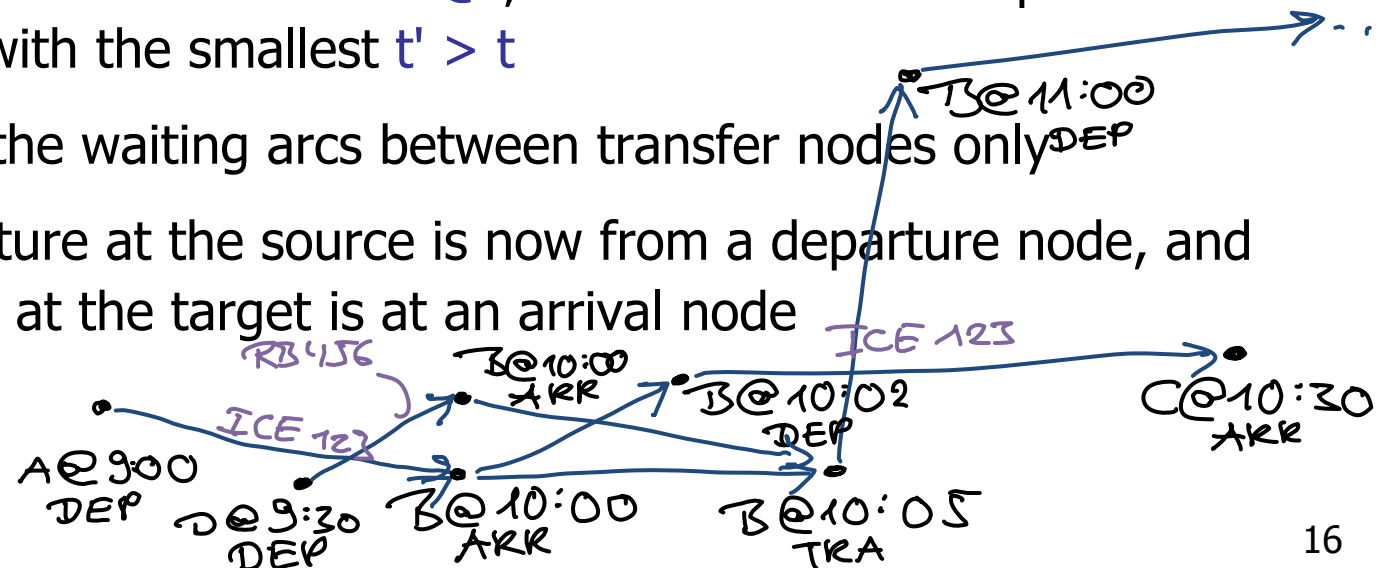
- This is non-trivial, because we need to distinguish between staying on a vehicle at a station (which must not require any transfer time) and changing the vehicle, for example:



# Transfer buffers 2/5

## ■ Time-expanded model, solution

- Split up each node from before into an **arrival node** and a **departure node**, and add an arc between the two (we can also model layover time that way now)
- For each arrival node  $A@t$ , add a **transfer node**  $A@t'$  and an arc from  $A@t$  to  $A@t'$ , where  $t' - t$  is the transfer buffer
- For each transfer node  $A@t$ , add an arc to the departure node  $A@t'$  with the smallest  $t' > t$
- Have the waiting arcs between transfer nodes only
- Departure at the source is now from a departure node, and arrival at the target is at an arrival node





- Time-dependent model, solution 1
  - We also have to distinguish here between staying on a vehicle and changing the vehicle at a station
  - It looks like we can do this by simply remembering for each node, along with the tentative arrival time  $t[u]$ , the id  $\ell$  of the vehicle with which we arrive at  $u$
  - Then we can build the transfer buffer into the cost function
$$\text{cost}_{u,v}(t, \ell) = \text{time to reach } v, \text{ if we are at } u \text{ at time } t \text{ sitting in vehicle } \ell$$
  - Unfortunately, Dijkstra's algorithm will not always correctly compute the shortest path anymore then

# Transfer buffers 4/5

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- Time-dependent model, problem

- Time-dependent model, solution 2
  - Have separate arrival and departure nodes, too
  - One arrival and one departure node per line suffices
  - But still, we no longer only have one node per station
- Time-dependent model, solution 3
  - When we can arrive at a station at two different times  $t_1$  and  $t_2$  with different vehicles, and  $|t_2 - t_1|$  is  $\leq$  the transfer buffer, pursue both possibilities
  - Then we need to do a multi-label Dijkstra (Dijkstra maintaining several shortest paths to the same node), see next lecture

## ■ General Transit Feed Specification

- Standard format established by Google in 2005
- Here is a nice story about it: <http://tinyurl.com/6yczek2>
- See the references to the GTFS specification
- Relatively complex, because there are so many peculiarities, special cases, etc. for transit networks
- For a simple graph model, it is easy though

## ■ Basic concepts

- stop = what we call a station
  - e.g. **Freiburg Hbf** or **Bertoldsbrunnen**
- trip = journey of a particular vehicle at a particular time
  - e.g. the journey of **Bus 11** from **Munzinger Straße** at **9:28** to **Paduaalle** at **10:11**
- route = trips that have a common description
  - e.g. all journeys of **Bus 11** over the day
- service days = days of the week when a trip is available
  - e.g. on **weekdays** (Mo-Fr) or on the **weekend** (Sa-Su)

- The files we need for exercise sheet #7
  - [stop\\_times.txt](#) : the actual schedule information, what eventually becomes the arcs in the transit graph
  - [frequencies.txt](#) : some lines repeat in exactly the same way over the same day, then you have the schedule only once in [stop\\_times.txt](#), and the periodicity here
  - [calendar.txt](#) : service day patterns, and which days of the week belong to it
  - [trips.txt](#) : tells us which trips commute on which service days (via the patterns from [calendar.txt](#))
  - All files are in [CSV](#) format = a table with one record per line, columns separated by a comma, headings in first line

- Write a class `CsvParser`

- With a method `readNextLine()` that reads the next line from the file and makes the columns available via another method `getItem(int i)`
- You find my `CsvParser.h` and `CsvParserTest.cpp` in the course `SVN` under folder `lectures`
- Note: for efficiency reasons, I let my `getItem` method return a `const char*` which points to part of an internal string object containing the last line read

It's slightly easier if you just return an `std::string`, but then you get one or two additional copies / allocations

## ■ Graph class

- If you have a graph class with members

```
vector<Node> _nodes;
```

```
vector<vector<Arc> > _adjacencyLists;
```

you can use that for the (time-expanded) transit network as well

- That way, you can run your algorithms with little or no modifications on the transit network as well
- You might want to add some additional info to the `Node` class (like the station to which a node belongs) and to the `Arc` class (like the name of the GTFS route)



# Implementation Advice 3/7

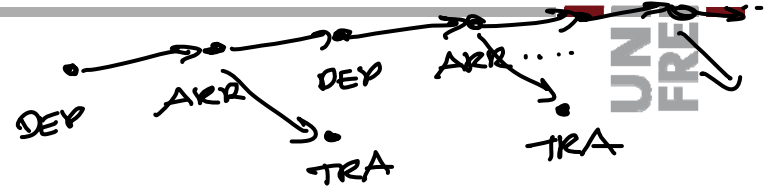
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- Parse the GTFS files in this order and way
  - First parse `calendar.txt` and remember (in a hash set) those service ids which contain the given weekday
  - Then parse `trips.txt` and remember (in a hash set) those trip ids with a valid (= remembered) service id
  - Then parse `stops.txt` and store (in a hash map) the names and coordinates by stop id
  - Then parse `frequencies.txt` and store by trip id
  - Then parse `stop_times.txt` and for each block of lines in the file with the same trip id, add the corresponding nodes and arcs to your graph

- Blocks with same trip id in `stop_times.txt`
  - For the last step, it is very convenient to have all lines with the same trip id together in one block, and within this block have them sorted by `stop_sequence`
  - You can easily achieve this with a command-line sort  
`sort -t, -k1,1r -k5,5n stop_times.txt > new_file.txt`
  - If you have frequency information for the trip id of a line from `stop_times.txt`, repeat accordingly, for example:

# Implementation Advice 5/7

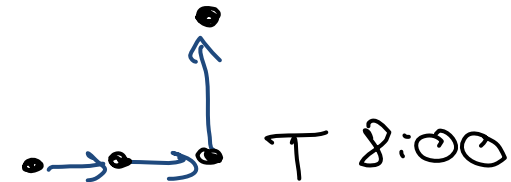
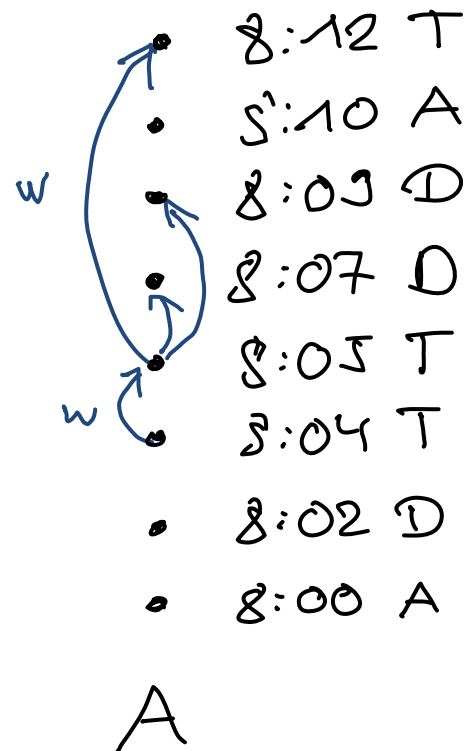
## ■ Arrival, departure, transfer nodes



- Create all nodes already while processing `stop_times.txt`
- And also the arcs from arrival to departure nodes and vice versa, and from arrival nodes to transfer nodes
- While processing `stop_times.txt`, maintain (in a hash map) for each station the list of nodes of that station, their time, and their type (arrival, departure, transfer)
- After processing `stop_times.txt`, for each station do:
  - Sort the nodes by time; then it is easy to add the missing arcs **from** the transfer nodes (waiting arcs to the next transfer node, and boarding arcs to the next departure node)
  - Beware: several nodes with exactly the same time

# Implementation Advice 6/7

- Arcs from transfer nodes, example



- Tricks to save some arcs
  - We can trivially **contract** all **departure** nodes
  - This replaces pairs of a boarding and a traveling arc by a single arc ... and actually **decrease** the total number of arcs in the graph, for example:

# Road vs. Transit Networks

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- Assume the time-expanded model
  - Then we can all our algorithms so far also for transit networks
  - But will the speed-up over ordinary Dijkstra be the same?

# References

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- Transit network models

Timetable information: Models and Algorithms

Müller-Hannemann, Schulz, Wagner, Zaroliagis, ATMOS 2007

<http://www.springerlink.com/content/x54715k627860283/>

- Road Networks vs. Transit Networks

Car or Public Transport — Two Worlds

Hannah Bast, Efficient Algorithms 2009, LNCS 5760

<http://www.springerlink.com/content/y46257m66372x730/>

- GTFS

– [http://code.google.com/transit/spec/transit\\_feed\\_specification.html](http://code.google.com/transit/spec/transit_feed_specification.html)

