

# Efficient Route Planning

## SS 2012

Lecture 9, Wednesday July 4<sup>th</sup>, 2012  
(Transit Networks, GTFS)

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# Overview of this lecture

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## ■ Organizational

- Your feedback from [Exercise Sheet #8 \(Transit Node Routing\)](#)

## ■ Transit Networks

- In the US, "transit" means "public transportation"
- Transit node routing has nothing to do with this "transit"
- We will see how to model a [transit network](#)
- [GTFS](#) = General Transit Feed Specification
- Do our algorithms so far work on transit networks?
- [Exercise Sheet #9](#): Parse a transit network from [GTFS](#) and run [1000](#) queries on it, using basic Dijkstra

# Feedback on ES#8 (Transit Node Routing)

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- Summary / excerpts last checked July 4, 15:05
  - Not hard for those with a working CH implementation
  - Otherwise most time used for fixing bugs in old code
  - Not a good idea to make the exercise sheets depending upon each other ... *sorry, but it's hard to avoid for this stuff*
    - But next sheets will be something completely new!
  - Why store transit nodes in a hash set?

# Results for ES#8 (Transit Node Routing)

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## ■ Summary

- Average time to compute access nodes:
  - $\sim 1\text{ms}$  for both datasets
  - That would be  $\sim 1\text{ hour}$  for the whole of BaWü
- Average number of access nodes
  - 6 for Saarland, 36 for BaWü
- Average query time
  - $\sim 10\ \mu\text{s}$  with C++, 2-3 times slower with Java
  - **Note:** the query times you measured benefit from the fact that all the relevant values are already in the cache

# Transit Networks

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- What kind of data have we got?
  - **Stations** (train stations, bus stops, etc.)
  - **Lines** (trains, buses, trams, etc.)
  - The **schedule** of these lines, that is, on which days do they serve which stations at which times
  - How to model these as a directed graph?
    - So that "from **A** to **B**" queries become shortest path queries on such a graph, just like for road networks

# Time-dependent model 1/2

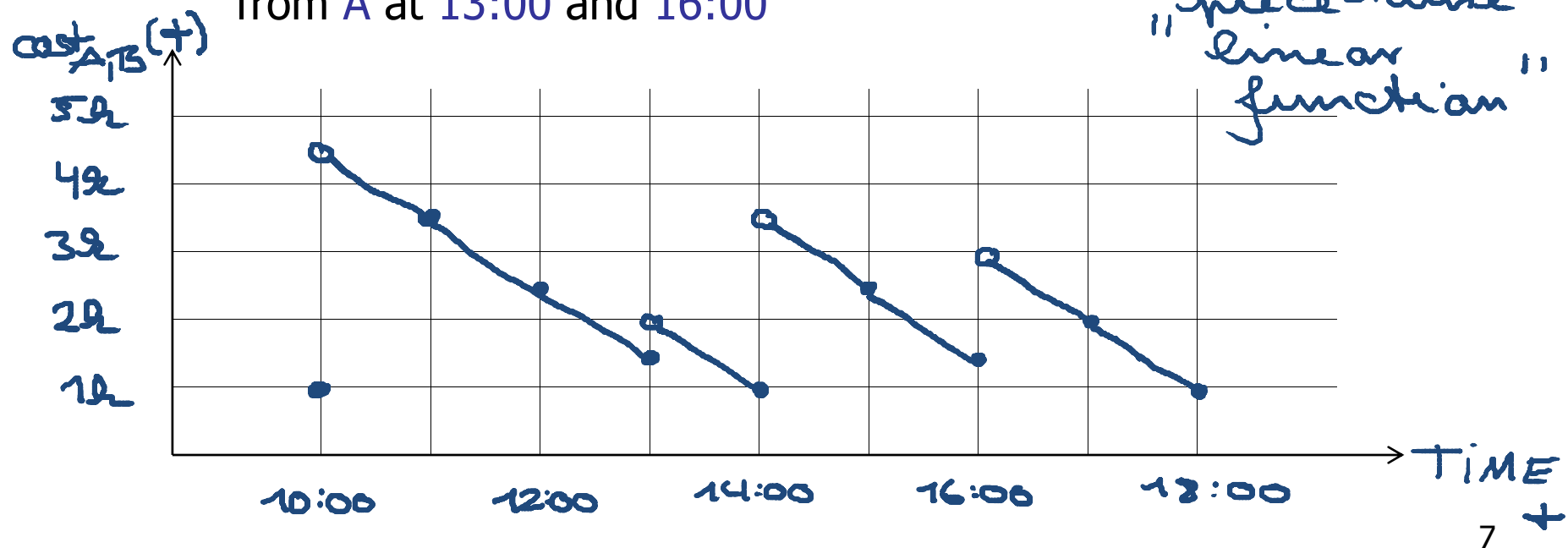
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- The first thing that comes to mind
  - Each station is a **node**
  - There is an **arc** between two nodes **u** and **v**, if there is a vehicle (train, bus, tram, ...) going **non-stop** from **u** to **v**
  - However, that arc can only be used at certain times, and the time it takes to travel across the arc depends on the vehicle commuting at that time
  - We can model this via a **cost function** for each arc **(u, v)**  
 $\text{cost}_{u,v}(t)$  = the time to get from **u** at time **t** ... to **v**
  - **Note:** for road networks that function was a constant

# Time-dependent model 2/2

## ■ Example

- Stations **A** and **B** with two lines **L1** and **L2**
- **L1** takes **1** hour from **A** to **B** (non-stop) and departs from **A** at **10:00**, **14:00** and **18:00**
- **L2** takes **1.5** hours from **A** to **B** (non-stop) and departs from **A** at **13:00** and **16:00**



# Time-dependent Dijkstra 1/2

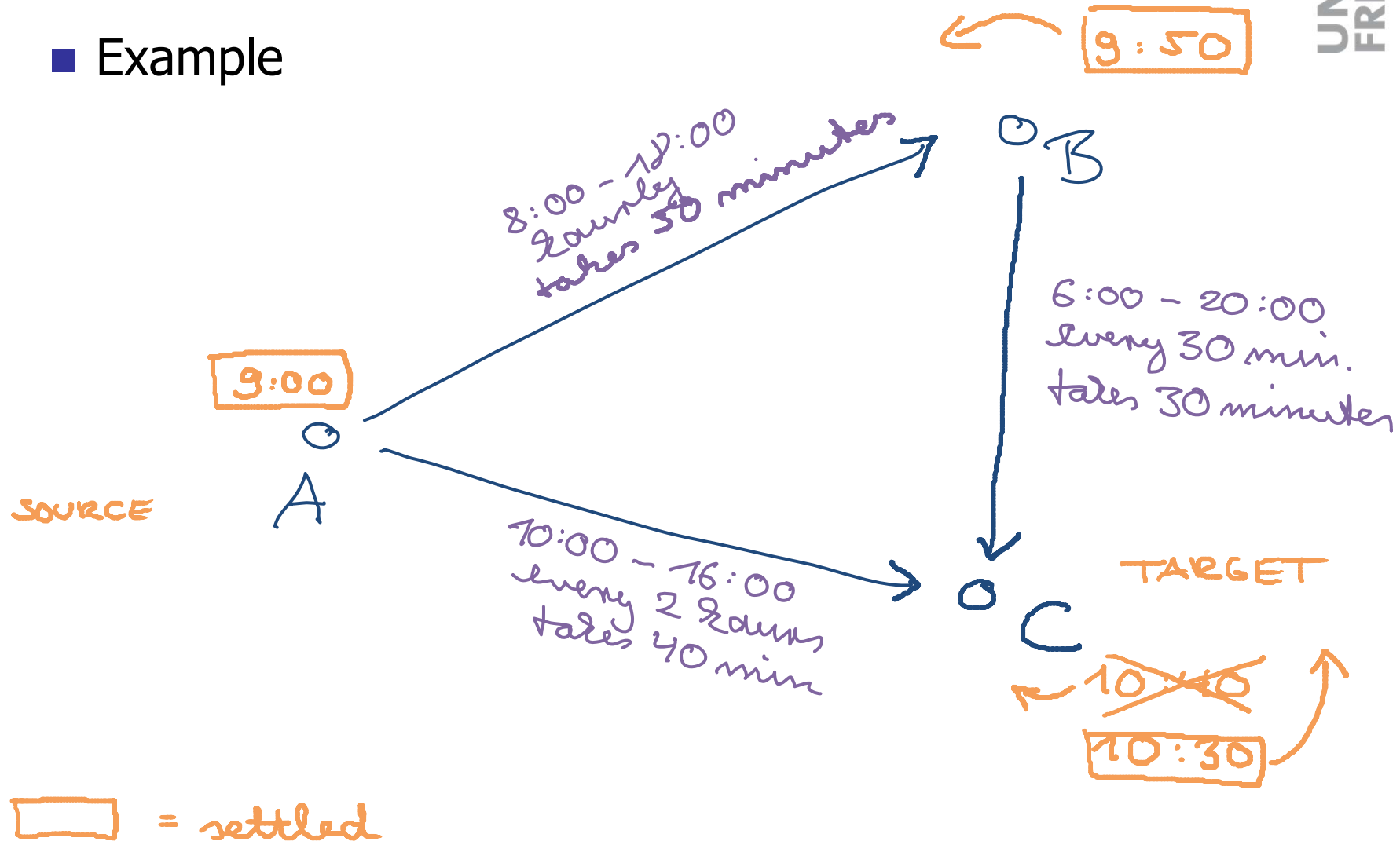
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- How to compute shortest paths on such a graph?
  - A simple variant of Dijkstra's algorithm does it
  - Tentative distances at the nodes are now **times of day**
    - We will store **absolute** times (like 10:20) and call them  $t[u]$  for node  $u$ , but we could also store times relative to the start time (like 40 minutes)
  - Start with  $t[s] = \text{start time}$  and all other  $t[u] = \infty$
  - When relaxing an arc  $(u, v)$  we compute  $c = c_{u,v}(t[u])$  and take  $t[v] = t[u] + c$  if that improves on the previous  $t[v]$
  - As for ordinary Dijkstra process the node  $u$  with the smallest  $t[u]$  next, and stop when this is the target node



# Time-dependent Dijkstra 2/2

## ■ Example



# Time-expanded model 1/3

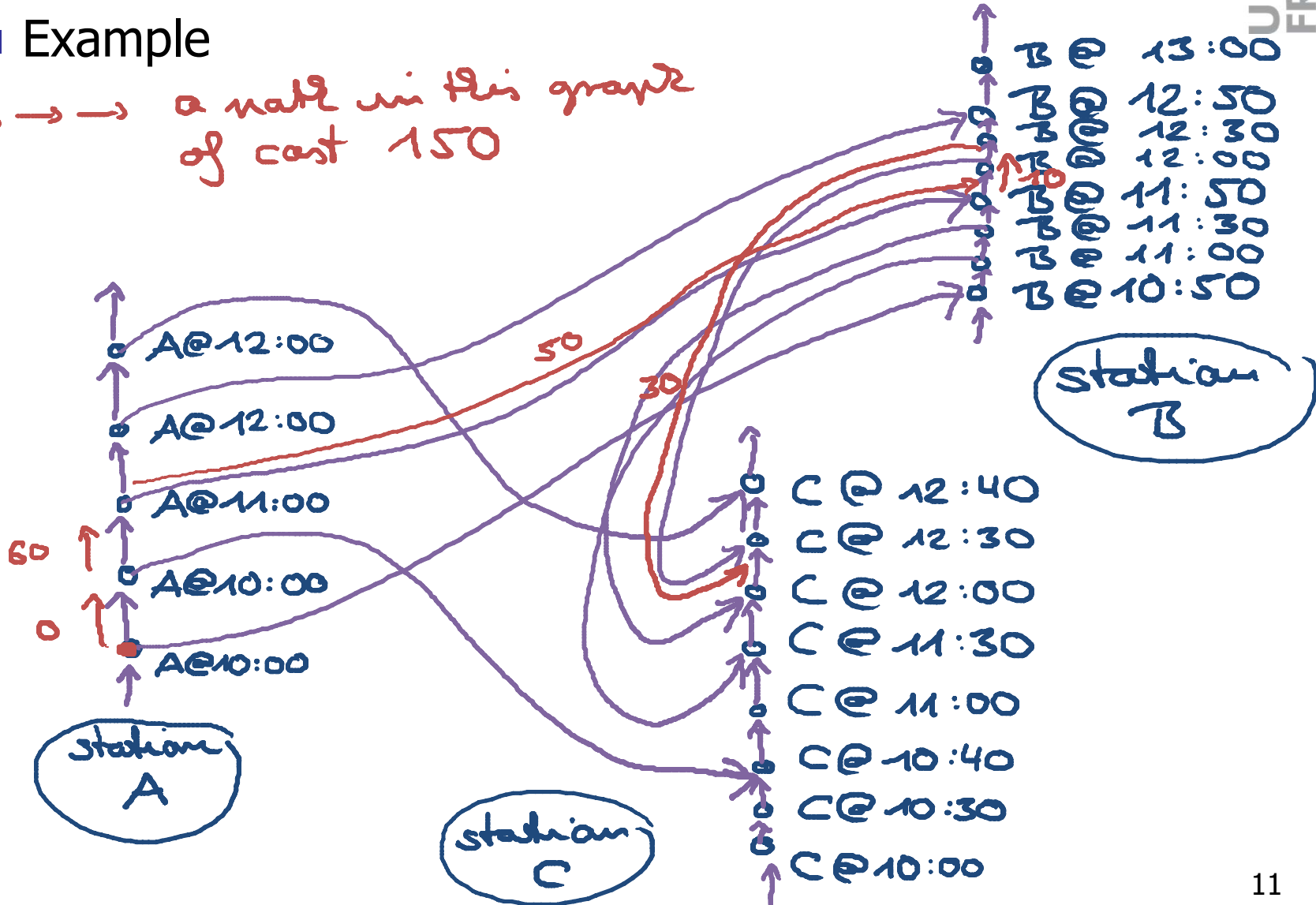
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- A node = a particular time at a particular station
  - Only at times, where something (= an arrival or a departure) is happening
  - For example, Freiburg Hbf @ 10:57
  - There is an arc between two nodes  $A@t_1$  and  $B@t_2$  if there is a vehicle departing from  $A$  at time  $t_1$  and arriving at  $B$  at time  $t_2$ , without stops inbetween
  - The cost of the arc is simply the travel time  $t_2 - t_1$
  - There is also an arc from  $A@t_1$  to that node  $A@t_2$  with the smallest  $t_2$  after  $t_1$  ... we call these **waiting** arcs

# Time-expanded model 2/3

## ■ Example

→ → → a node in this graph of cost 150



# Time-expanded model 3/3

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- How do we compute shortest paths in this model?
  - It's an ordinary directed graph with (static) non-negative arc costs, so we can use ordinary Dijkstra
  - **Problem:** We do not have a target node, we only have a target station
  - **Solution:** Run Dijkstra until **any** node from the target station is settled (which will be the first one reached)

# Time-expanded vs. time-dependent

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- So far, not much difference
  - Given a query  $A@t \rightarrow B$ , consider the sequence of arcs relaxed by a (time-dependent) Dijkstra on the time-dependent graph
  - The Dijkstra on the time-expanded graph relaxes the same arcs in the same order
    - **plus** some additional waiting arcs to some additional nodes and the arcs leaving from these nodes
  - Intuitively, the time-dependent Dijkstra considers waiting and normal arcs in one (time-dependent) arc
  - The big advantage of the time-expanded model is that we have an ordinary directed graph and can thus use **all** our previous algorithms on it

# Advanced modelling issues

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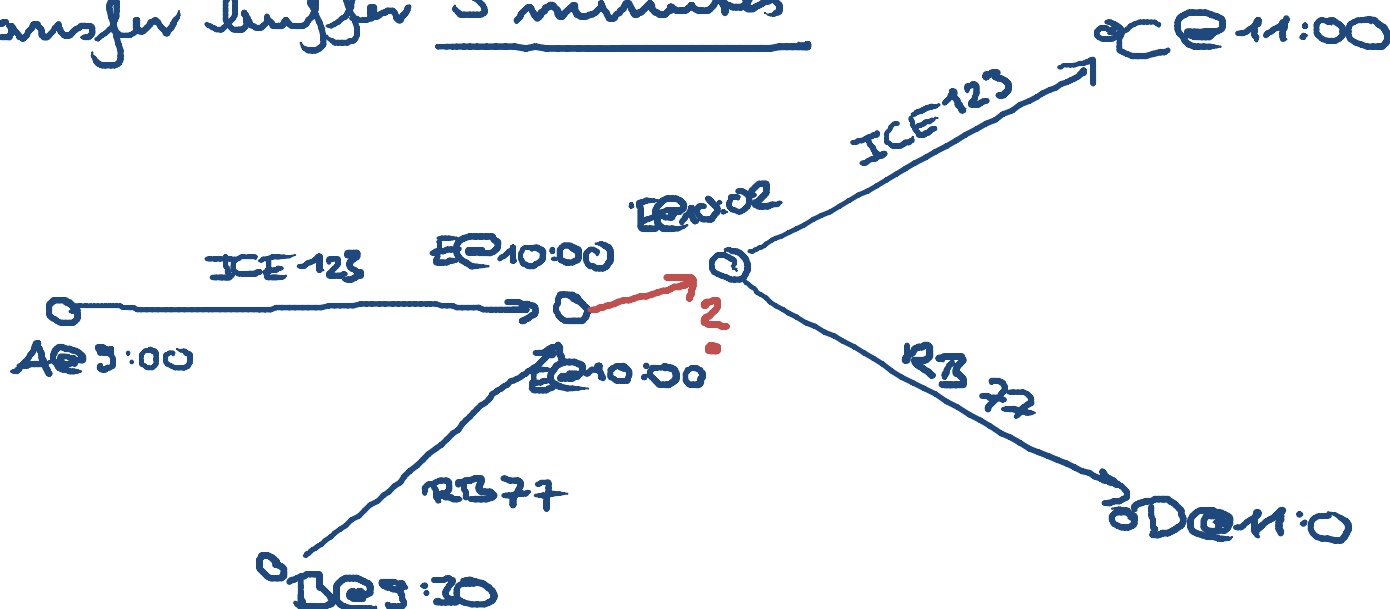
- For example, what about ...
  - Transfer buffers
    - We need a minimal amount of time to transfer between two vehicles → next slide
  - Service days
    - Different schedules on different weekdays, holidays, etc. → later slide
  - Multi-criteria cost functions
    - Maybe we can get from A@t to B in 3 hours with 0 transfers, or in 2 hours with 2 transfers
    - Which one is better depends on user preference, so we should compute both → next lecture

# Transfer buffers 1/6

## ■ Time-expanded model

- This is non-trivial, because we need to distinguish between
  - staying on a vehicle at a station (no transfer buffer)
  - changing the vehicle (non-zero transfer buffer)

let's say  
transfer buffer 5 minutes



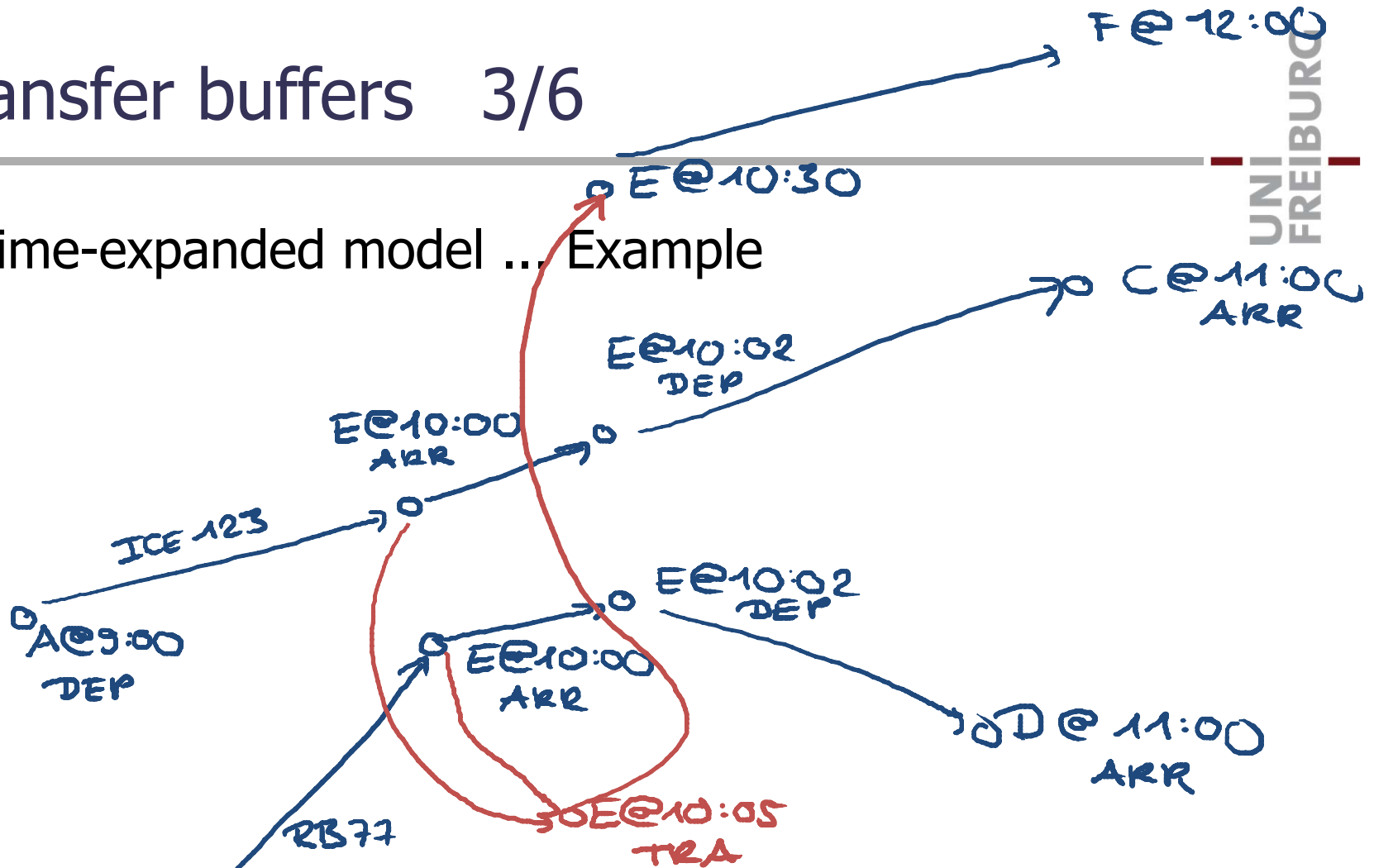
## ■ Time-expanded model ... Solution

- Split up each node from before into an **arrival node** and a **departure node**, and add an arc between the two
  - we can also model layover time that way now!
- For each arrival node  $A@t$ , add a new **transfer node**  $A@t'$  where  $t' = t + \Delta$  ... where  $\Delta$  is the transfer buffer
- For each departure node  $A@t$  have an arc from the transfer node  $A@t'$  with the largest  $t'$  that is  $\leq t$
- Have the waiting arcs between transfer nodes only
- Departure at the source is now from a departure node, and arrival at the target is at an arrival node



# Transfer buffers 3/6

## ■ Time-expanded model ... Example

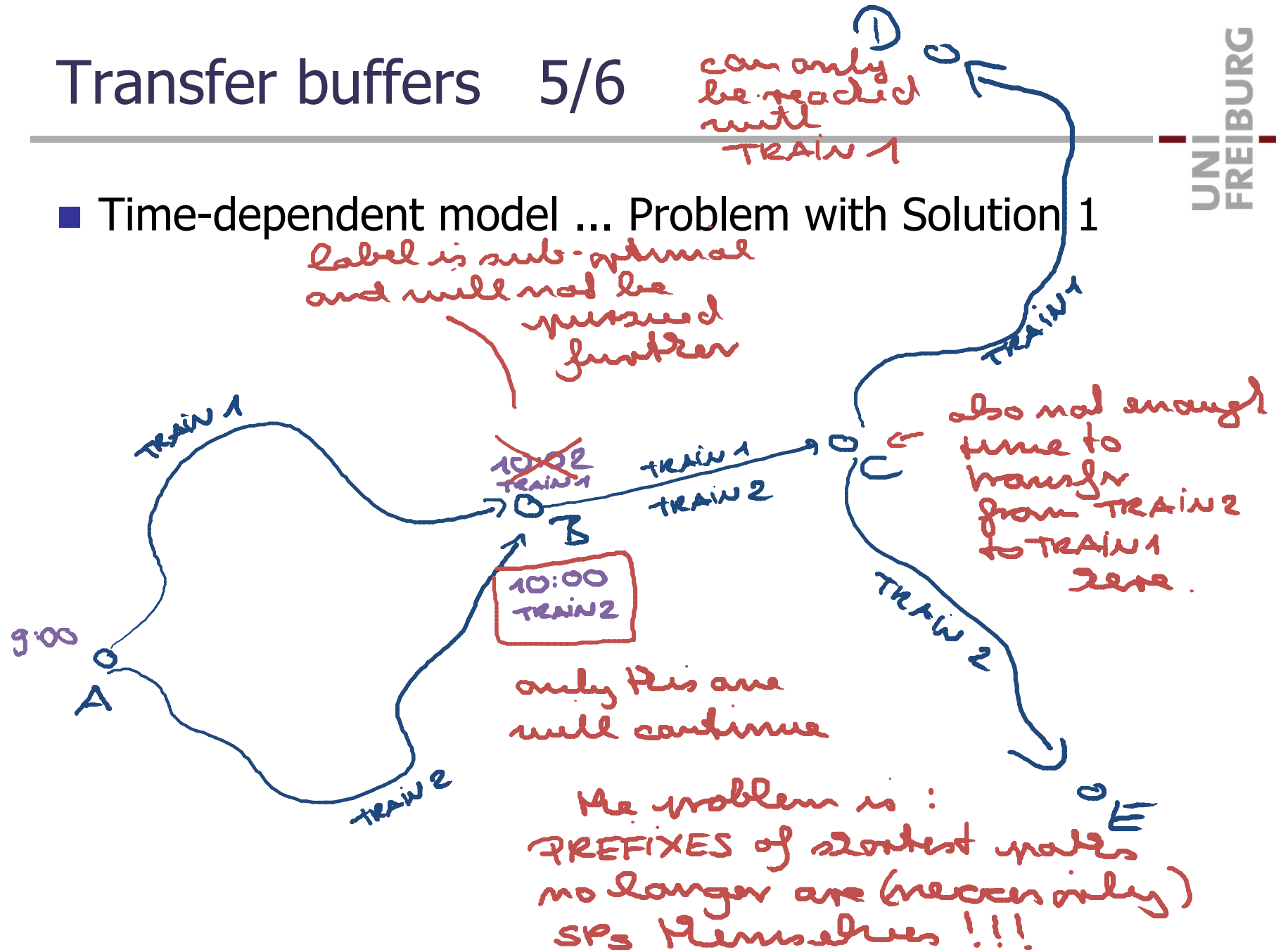


DEP → ARR : "traveling"  
ARR → DEP : "layover"  
ARR → TRA : "alighting"  
TRA → DEP : "boarding"

- Time-dependent model ... Solution 1
  - We also have to distinguish here between staying on a vehicle and changing the vehicle at a station
  - It looks like we can do this by simply remembering for each node, along with the tentative arrival time  $t[u]$ , the id  $\ell$  of the vehicle with which we arrive at  $u$
  - Then we can build the transfer buffer into the cost function
$$\text{cost}_{u,v}(t, \ell) = \text{time to reach } v, \text{ if we are at } u \text{ at time } t \text{ sitting in vehicle } \ell$$
  - Unfortunately, it can happen then that Dijkstra's algorithm **misses** some shortest paths

# Transfer buffers 5/6

## Time-dependent model ... Problem with Solution 1



## ■ Time-dependent model ... Solution 2

- When we can arrive at a station at two different times  $t_1$  and  $t_2$  with different vehicles, and  $|t_2 - t_1|$  is  $\leq$  the transfer buffer, pursue **both** possibilities
- Then we need to do a **multi-label Dijkstra** (maintains sets of labels per node) ... **see next lecture**

## ■ Time-dependent model ... Solution 3

- Have separate arrival and departure nodes, too
- One arrival and one departure node per "line" suffices
  - less nice, since no longer only one node per station
  - but often a good compromise in practice

- General Transit Feed Specification
  - Standard format established by Google in 2005
  - The story how it started: <http://tinyurl.com/6yczek2>
  - See the references to the GTFS specification
  - Relatively complex, because there are so many peculiarities, special cases, etc. for transit networks
  - For a simple graph model, it is easy though

## ■ Basic concepts

- **stop** = what we call a station
  - e.g. **Freiburg Hbf** or **Siegesdenkmal**
- **trip** = journey of a particular vehicle at a particular time
  - e.g. the journey of **Bus 10** from **Bärenweg** at **17:56** to **Siegesdenkmal** at **18:07**
- **route** = trips that have a common description (our "line")
  - e.g. all journeys of **Bus 10** over the day
- **service days** = days of the week when a trip is available
  - e.g. on **weekdays** (Mo-Fr) or on the **weekend** (Sa-Su)

- The files you need for **Exercise Sheet #9**
  - **stop\_times.txt** : the actual schedule information, what eventually becomes the arcs in the transit graph
  - **frequencies.txt** : some lines repeat in exactly the same way over the same day, then you have the first trip in **stop\_times.txt**, and how it repeats in **frequencies.txt**
  - **calendar.txt** : service day patterns, and which days of the week belong to it
  - **trips.txt** : tells us which trips commute on which service days (via the patterns from **calendar.txt**)
  - All files are in **CSV** format = a table with one record per line, columns separated by a comma, headings in first line

- You need a simple CSV Parser
  - We have written one for you in both C++ and Java
    - because we are so incredibly nice
  - You find it in the SVN folder for this lecture
  - Very simple and easy-to-use interface
    - `openFile(csvFileName)` ... open the CSV file
    - `readNextLine()` ... read next line from file
    - `getItem(i)` ... get column `i` of line just read



## ■ Graph class

- If you have a graph class with members

```
Array<Array<Arc>> adjacentArcs;  
Array<Node> nodes;
```

you can use that for the (time-expanded) transit network as well

- That way, you can run your algorithms with little or no modifications on the transit network as well
- You might want to add some additional info to the `Node` class (like the station to which a node belongs) and to the `Arc` class (like the name of the GTFS route)

# Implementation Advice 3/7

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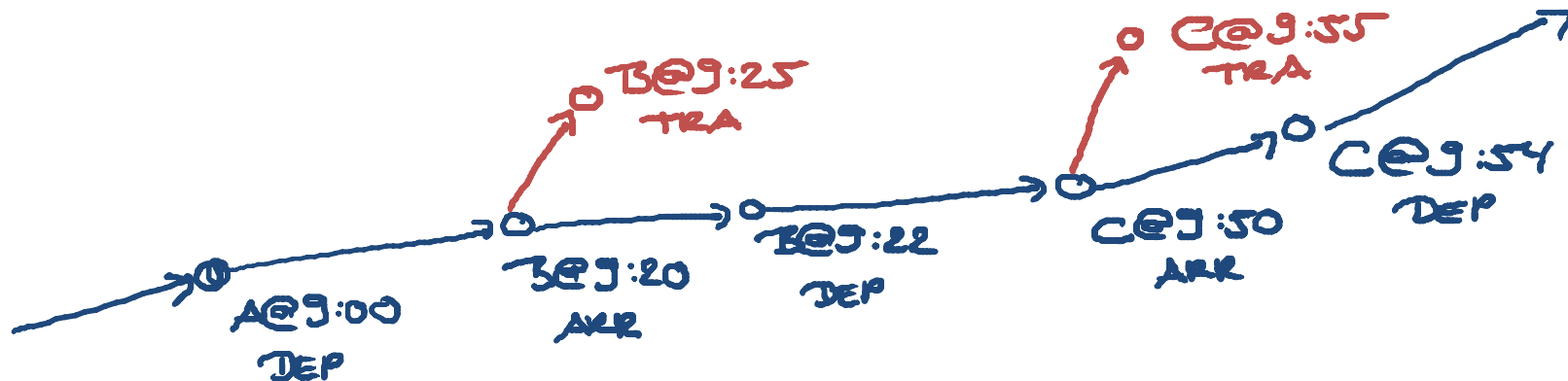
- For the graph on a given weekday, do as follows:
  - First parse `calendar.txt` and remember (in a hash set) those service ids which contain the given weekday
  - Then parse `trips.txt` and remember (in a hash set) those trip ids with a valid service id from the hash set above
  - Then parse `stops.txt` and create a mapping from the GTFS stop id strings to consecutive numerical stop ids
  - Then parse `frequencies.txt` and store (in a hash map) the repetitions for each trip id ... **not needed for Exercise!**
  - Then parse `stop_times.txt` and for each block of lines in the file with the same trip id, add the corresponding nodes and arcs to your graph ... **see following slides**

- Blocks with the same trip id in `stop_times.txt`
  - For the last step, it is very convenient to have all lines with the same trip id together in one block, and within this block have them sorted by `stop_sequence`
  - The `GTFS` standard does not demand this ... but you can easily achieve this with a command-line sort

```
sort -t, -k1,1r -k5,5n stop_times.txt > new_file.txt
```
  - If you have frequency information for the trip id of a line from `stop_times.txt`, don't forget to repeat accordingly
    - **Note:** some GTFS feeds write all times explicitly in `stop_times.txt` and do not have `frequencies.txt` at all
    - In particular, this is so for the GTFS feed from `ExSh#9`

# Implementation Advice 5/7

- Arrival, departure, transfer nodes ... **Step 1a**
  - While parsing `stop_times.txt` create the following arcs
    - between arrival and departure nodes ("traveling arcs")
    - from arrival nodes to transfer nodes ("alighting arcs")
  - Create the corresponding nodes at the same time
  - **Note:** you can use entirely new nodes for each trip ... there is no need to share nodes between different trips



## ■ Arrival, departure, transfer nodes ... **Step 1b**

- While parsing `stop_times.txt`, also maintain for each station the list of arrival and transfer nodes of that station, with their time and type (arrival or transfer)

```
Array<Array<Node>> nodesPerStation;
```

- In `GTFS` the station ids are strings, but better convert them to consecutive station ids during the parsing of `stops.txt` ... remember the correspondence like this:

```
HashMap<string, int> stationIdsByGtfsName;
```

- It remains to add the following arcs:
  - from transfer nodes to departure nodes ("boarding arcs")
  - from one transfer node to the next ("waiting arcs")

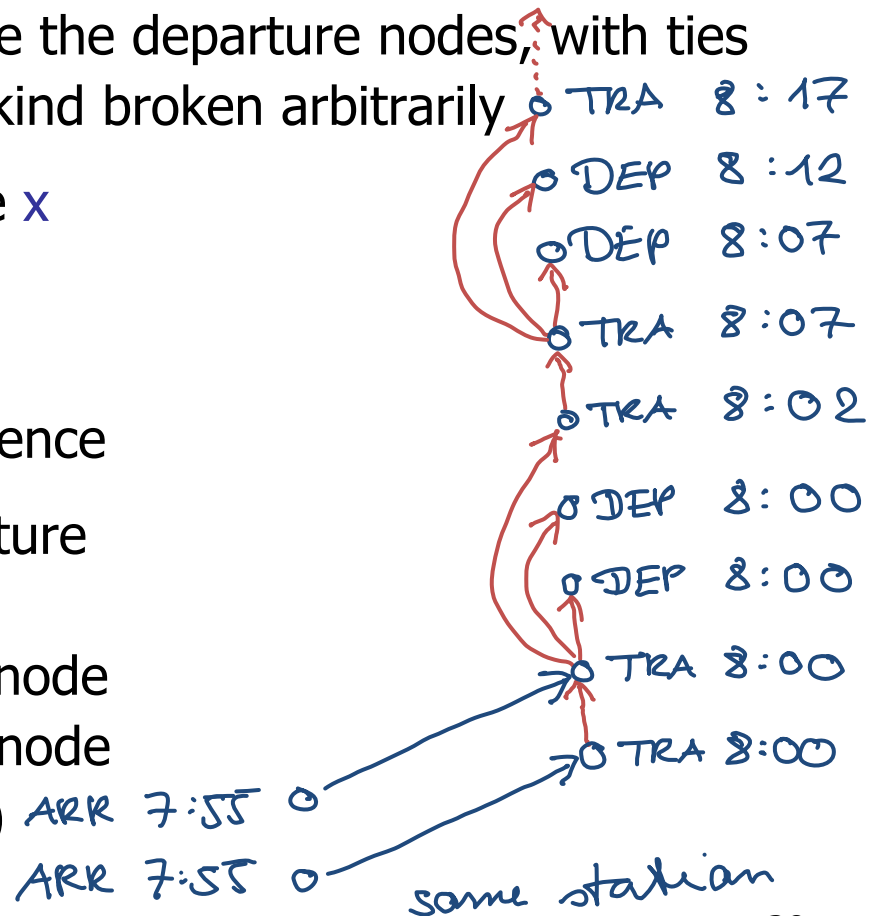
# Implementation Advice 7/7

## ■ Arrival, departure, transfer nodes ... Step 2

- For each station: sort the nodes by time, and for equal times, sort the transfer nodes before the departure nodes, with ties between nodes of the same kind broken arbitrarily

- Then for each **transfer** node  $x$  in the sorted sequence

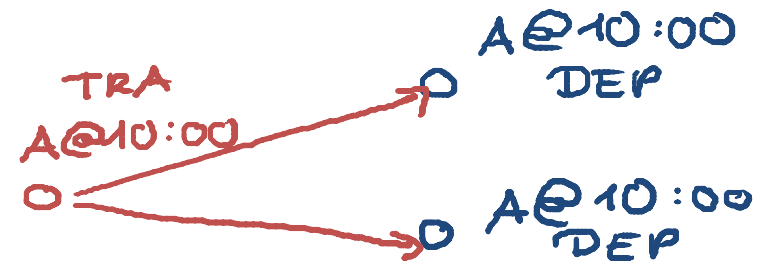
- add an arc to the next transfer node in the sequence
- add an arc to each departure node that comes after  $x$  without another transfer node in between (none, if next node after  $x$  is a transfer node)



# Some simple optimizations (not needed for Exercise)

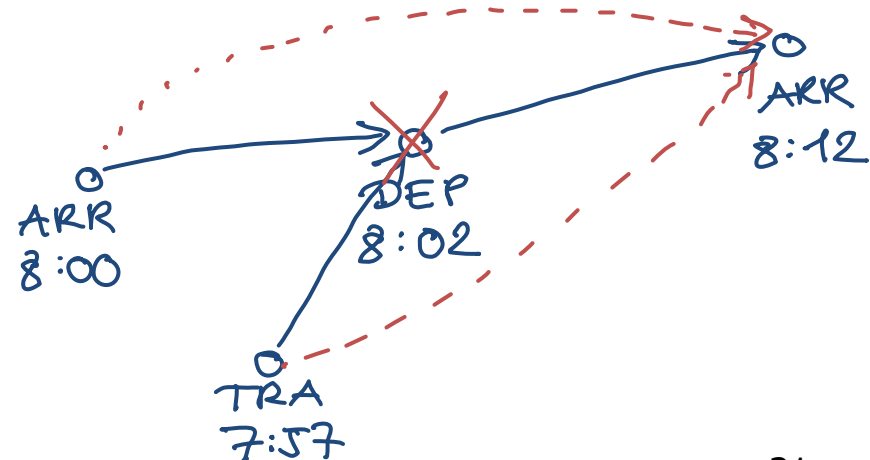
## ■ Less transfer nodes

- If a station has several departure nodes at the same time, it suffices to add a single transfer node for all of them



## ■ Contract departure nodes

- This decreases the number of arcs that were incident to the departure nodes by a factor of  $3/2$



# Road vs. Transit Networks

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- Assume the time-expanded model
  - Then we can run all our algorithms so far also for transit networks ... and they will correctly compute shortest paths
  - But will the speed-up over ordinary Dijkstra be the same?
  - We will look at that in the next lecture ...



# References

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- Transit network models

Timetable information: Models and Algorithms

Müller-Hannemann, Schulz, Wagner, Zaroliagis, ATMOS 2007

<http://www.springerlink.com/content/x54715k627860283/>

- GTFS

- <https://developers.google.com/transit/gtfs/>

- <http://www.gtfs-data-exchange.com/>

